

# Dimensionless Free Vibration Analysis of Suspension Bridges Considering Hanger Extensibility and Various Girder Types

## Dong-Ho CHOI

Professor, Ph.D.  
Dept. of Civil and  
Environmental Eng.  
Hanyang University  
Seoul, Korea  
[samga@hanyang.ac.kr](mailto:samga@hanyang.ac.kr)

Dong-Ho Choi, born 1963, received his Ph.D. degree from MIT in 1997. His main research includes cable-supported bridges and steel structures.



## Sun-Gil GWON

Ph.D. Candidate  
Dept. of Civil and  
Environmental Eng.  
Hanyang University  
Seoul, Korea  
[verysoon@hanyang.ac.kr](mailto:verysoon@hanyang.ac.kr)

Sun-Gil Gwon, born 1985, received his Master's degree from Hanyang University in 2011.



## Summary

In this paper, free vibration analyses with an improved continuum model for three-span suspension bridges are performed to study the effects of hanger extensibility on free vertical vibrations. The improved model can consider extensible hangers as well as various girder types such as hinged, continuous, and floating girders. To derive the equations of motion for this model, the coupled differential equations for the vertical deflections of the main cable and girder are presented. The Galerkin's method with the shape functions for the main cable and girder is introduced into the differential equations, and it leads the equations to a matrix form. The natural frequencies of a three-span suspension bridge are evaluated from the equations with the six dimensionless parameters. In the parametric analyses, the effect of the hanger extensibility is observed.

**Keywords:** Suspension bridge; Free vibration; Continuum model; Extensible hanger; Girder type.

## 1. Introduction

A continuum model based on the deflection theory is useful in a preliminary design of a suspension bridge because it does not need an initial equilibrium state analysis and can identify key design parameters. However, most of the conventional continuum models assume inextensible hangers while hangers are actually extensible. In addition, the conventional models cannot consider a floating girder. Therefore, this paper presents an improved continuum model for three-span suspension bridges with extensible hangers and three girder types such as hinged, continuous, and floating girders. Dimensionless free vibration analyses using the improved model are then performed to study the effects of hanger extensibility on free vertical vibrations of the bridges.

## 2. Improved continuum model

Fig. 1 shows a suspended girder considered in this study. In Fig. 1,  $m_c$  and  $m_g$  are the uniform masses of the main cable and girder, respectively;  $g$  is the gravitational acceleration;  $E_c$  and  $A_c$  are the elastic modulus and the cross-sectional area of the main cable, respectively;  $E_h$  and  $A_h$  are the elastic modulus and the cross-sectional area of the hangers, respectively;  $E_g$  and  $I_g$  are the elastic modulus and the moment of inertia of

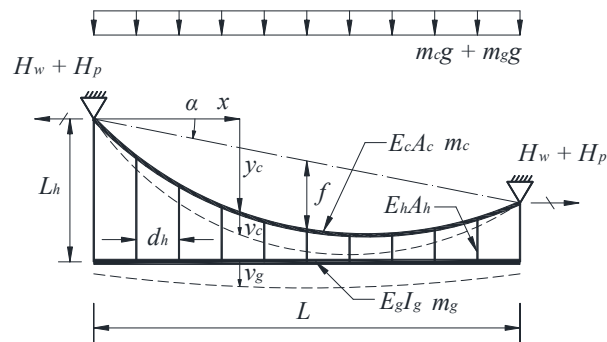


Fig. 1: Suspended girder with extensible hangers